



SENIOR PHASE

GRADE 9

NOVEMBER 2014

MATHEMATICS MEMORANDUM

MARKS: 100

Important information.

- This is marking guideline. In instances where learners have used different Mathematically sound strategies to solve the problems, they (learners) should be credited.
- Underline errors committed by learners and apply Consistent Accuracy (CA) marking.

Symbol	Explanation
M	Method mark
CA	Consistent Accuracy mark
A	Accuracy mark

This memorandum consist of 9 pages.

Ques.	Solution	Mark Allocation	Total
QUESTION 1			
1.1	C	Give 1 mark for each correct answer.	
1.2	D		
1.3	B		
1.4	C		
1.5	B		
1.6	D		
1.7	B		
1.8	B		
1.9	C		
1.10	C		
			[10]
QUESTION 2			
2.1	$13 \checkmark A$	13: 1 mark	(1)
2.2	$T_n = 3n + 1 \checkmark \checkmark A$ OR $T_n = 4 + 3(n - 1) \checkmark \checkmark A$	$3n$: 1 mark $+1$: 1 mark 4 : 1 mark $3(n - 1)$: 1 mark	(2)
2.3	$T_{20} = 3(20) + 1$ $= 61 \checkmark CA$ OR $T_{20} = 4 + 3(20 - 1)$ $= 61 \checkmark CA$	Answer: 1 mark	(1)
			[4]
QUESTION 3			
3.1	$(5^x)^0$ $= 1 \checkmark A$	1: 1 mark	(1)
3.2	$\frac{x}{2} - \frac{y}{3} + 1$ $= \frac{3x-2y}{6} + \frac{6}{6} \checkmark M$ $= \frac{3x-2y+1}{6} \checkmark A$	Same denominator: 1 mark $3x - 2y + 1$: 1 mark	(2)

3.3	$-(3x - 2)^2 + 4x$ $= -(9x^2 - 6x + 4) + 4x \quad \checkmark M$ $= -9x^2 + 6x - 4 + 4x \quad \checkmark M$ $= 9x^2 + 10x - 4 \quad \checkmark CA$	$9x^2 - 6x + 4$: 1 mark $-9x^2 + 6x - 4$: 1 mark $-9x^2 + 10x - 4$: 1 mark	(3)
			[6]
QUESTION 4			
4.1	$x^2 - 8x + 15$ $= (x - 3)\checkmark(x - 5) \quad \checkmark A$	$(x - 3)$: 1 mark $(x - 5)$: 1 mark	(2)
4.2	$\frac{1}{2}x^2 - 8$ $= \frac{x^2 - 16}{2} \quad \checkmark A$ $= \frac{(x-4)(x+4)}{2} \quad \checkmark A$	$\frac{x^2 - 16}{2}$: 1 mark $\frac{(x-4)(x+4)}{2}$: 1 mark	(2)
4.3	$x^2 + 3x + tx + 3t$ $= x(x + 3) + t(x + 3) \quad \checkmark M$ $= (x + 3)\checkmark(x + t) \quad \checkmark A$	Grouping: 1 mark $(x + 3)$: 1 mark $(x + t)$: 1 mark	(3)
			[7]
QUESTION 5			
5.1	$3x + 4 = 10$ $\frac{3x}{3} = \frac{10-4}{3} \quad \checkmark M$ $x = 2 \quad \checkmark A$	Calculation: 1 mark Answer: 1 mark	(2)
5.2	$\frac{x}{3} + \frac{x+5}{2} = 0$ $6\left(\frac{2x+3x+15}{6}\right) = 0 \times 6 \quad \checkmark M$ $5x + 15 = 0 \quad \checkmark M$ $5x = -15$ $x = -3 \quad \checkmark CA$	Multiply LHS and RHS by 6 Simplification: 1 mark Answer: 1 mark	(3)
5.3	$x^3 = 125$ $x^3 = 5^3 \quad \checkmark M$ $x = 5 \quad \checkmark A$ OR $x^3 = 125$ $x = \sqrt[3]{125} \quad \checkmark M$ $x = 5 \quad \checkmark A$	Calculation: 1 mark Answer: 1 mark	(2)
			[7]

QUESTION 6									
6.1	$1,7 \times 10^{13} \checkmark A$	Answer: 1 mark	(1)						
6.2	$90 \text{ km/h} = \frac{7}{2} h$ $\therefore x \text{ km/h} = 3 h$ $3 \times x \text{ km/h} \checkmark = 90 \times \frac{7}{2} \checkmark M$ Average speed = $105 \text{ km/h} \checkmark A$	$3 \times x \text{ km/h}: 1 \text{ mark}$ $90 \times \frac{7}{2}: 1 \text{ mark}$ Answer: 1 mark	(3)						
6.3	$S.I. = \frac{P.n.r}{100} \checkmark M$ $= \frac{R4\,400 \times 4 \times 7}{100} \checkmark M$ $= R1\,232.00 \checkmark CA$ OR $SI = Pni \checkmark M$ $= 4\,400 \times 7 \times 0,04 \checkmark M$ $= R\,1\,232,00 \checkmark CA$	Formula: 1 mark Substitution: 1 mark Answer: 1 mark	(3)						
6.4	$A = P(1 + \frac{r}{100})^n$ $= 5\,600P(1 + \frac{7}{100})^4 \checkmark M$ $= R7\,340,46 \checkmark CA$ OR $A = P(1 + i)^n$ $= 5\,600(1 + 0,07)^4 \checkmark M$ $= R7\,340,46 \checkmark CA$	Substitution: 1 mark Answer: 1 mark	(2)						
6.5	<table style="width: 100%; border: none;"> <tr> <td style="text-align: center;">now</td> <td style="text-align: center;">6yrs ago</td> </tr> <tr> <td style="text-align: center;">Son is x</td> <td style="text-align: center;">$x - 6$</td> </tr> <tr> <td style="text-align: center;">Father $3x$</td> <td style="text-align: center;">$3x - 6$</td> </tr> </table> $3x - 6 = 5(x - 6) \checkmark M$ $2x = 24 \checkmark M$ $x = 12$ Son = 12 years $\checkmark A$ Father = 36 years $\checkmark CA$	now	6yrs ago	Son is x	$x - 6$	Father $3x$	$3x - 6$	Correct statement: 1 mark Calculation: 1 mark 12 years: 1 mark 36 years: 1 mark	(4)
now	6yrs ago								
Son is x	$x - 6$								
Father $3x$	$3x - 6$								
			[13]						

QUESTION 7

7.1

$$X(-1; 4) \quad Y(0; 5)$$

$$m = \frac{y_2 - y_1}{x_2 - x_1} \checkmark M$$

$$m = \frac{5 - 4}{0 - (-1)}$$

$$= 1 \checkmark M$$

$$y\text{-intercept} = 5$$

$$y = mx + 5$$

$$= x + 5 \checkmark A$$

OR

$$Y(0; 5) \quad Z(1; 6)$$

$$m = \frac{y_2 - y_1}{x_2 - x_1} \checkmark M$$

$$m = \frac{6 - 5}{1 - 0}$$

$$= 1 \checkmark M$$

$$y\text{-intercept} = 5$$

$$y = mx + 5$$

$$= x + 5 \checkmark A$$

OR

$$X(-1; 4) \quad Z(1; 6)$$

$$m = \frac{y_2 - y_1}{x_2 - x_1} \checkmark M$$

$$m = \frac{6 - 4}{1 - (-1)}$$

$$= \frac{2}{2}$$

$$= 1 \checkmark M$$

$$y\text{-intercept} = 5$$

$$y = mx + 5$$

$$= x + 5 \checkmark A$$

Calculation: 1 mark

m = 1: 1 mark

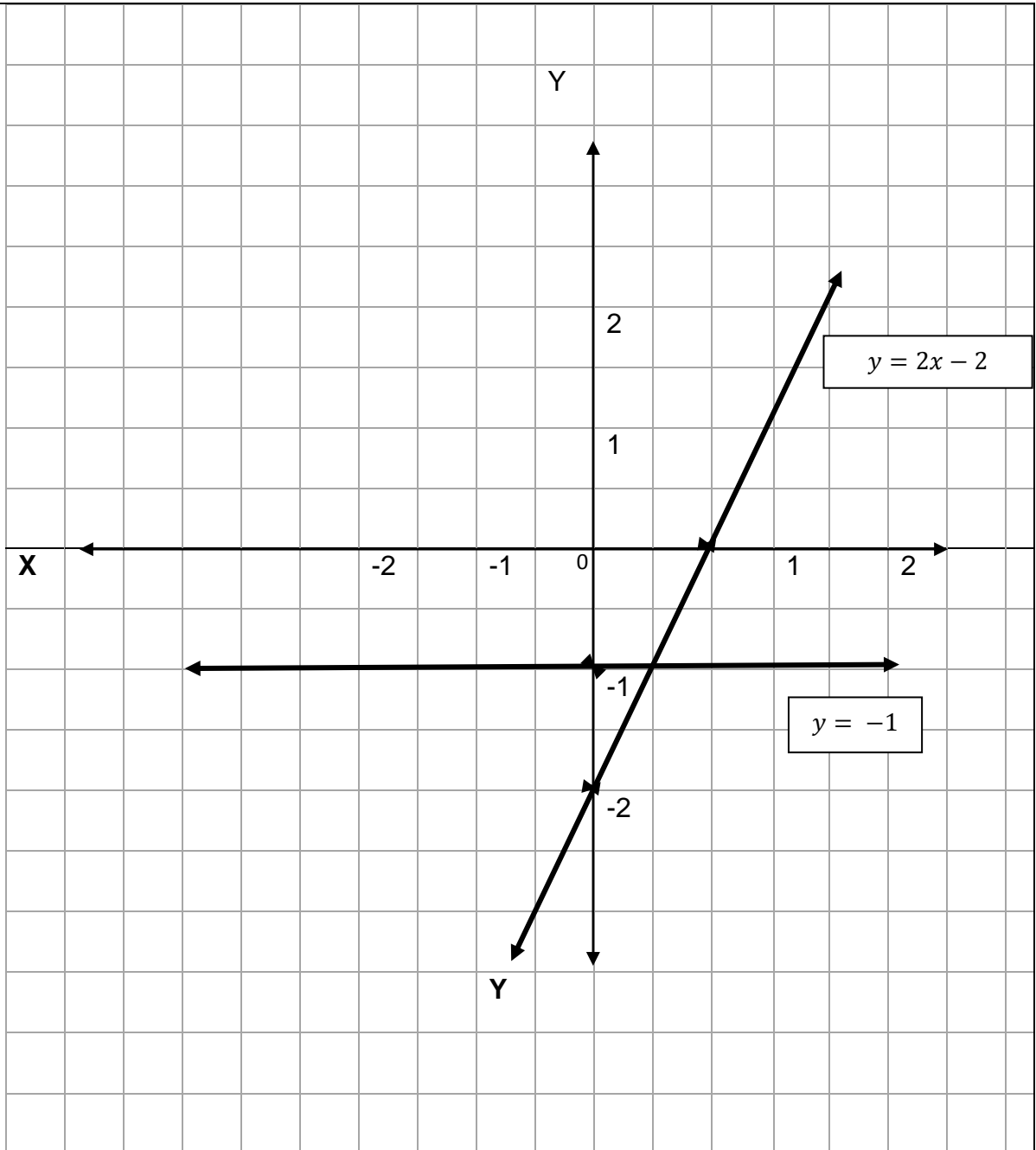
Answer: 1 mark

(3)

7.2

x	-2	-1	0	1	2
y = 2x - 1	-6	-4	-2	0	2
y = -1	-1	-1	-1	-1	-1

7.2



x-intercept : 1 mark ✓
y-intercept : 1 mark per graph ✓ + ✓
Labelling graph ✓ + ✓
(5)

[8]

QUESTION 8				
8.1	8.1.1	$\widehat{SRT} = \widehat{Q} = x + 70^\circ$ (corr. \angle s, $RT//QP$) \checkmark A $\widehat{S} + \widehat{TRS} + \widehat{P} = 180^\circ$ (sum of f \angle s of Δ) \checkmark A $x + 10^\circ + 28^\circ + 70^\circ = 180^\circ$ $2x + 108^\circ = 180^\circ$ $2x = 72^\circ$ \checkmark A $x = 36^\circ$ \checkmark A	<p>Correct statement with reason: 1 mark</p> <p>Correct statement with reason: 1 mark</p> <p>Simplification: 1 mark</p> <p>Answer: 1 mark</p>	(4)
	8.1.2	$\widehat{STR} = \widehat{P} = x + 10^\circ$ \checkmark A (corr. \angle s, $RT//QP$) \checkmark $A \widehat{STR} = 36^\circ + 10^\circ$ $= 46^\circ$ \checkmark A	<p>Correct statement: 1 mark</p> <p>Correct statement: 1 mark</p> <p>Answer: 1 mark</p>	(3)
	8.1.3	$\widehat{SRT} = \widehat{Q} = x + 70^\circ$ (corr. \angle s, $RT//QP$) $x + 70^\circ = 36^\circ + 70^\circ$ \checkmark A $= 106^\circ$ $106^\circ \neq 90^\circ$ $\therefore PQS$ is not a right angled triangle \checkmark A	<p>Correct statement: 1 mark</p> <p>Substitution: 1 mark</p> <p>Answer: 1 mark</p>	(3)
8.2	8.2.1	<i>In ΔABC and ΔTSP</i> $\widehat{B} = \widehat{P} = 70^\circ$ (given) \checkmark $\widehat{C} = \widehat{S} = 70^\circ$ (base \angle s of is os. Δ) \checkmark A $\widehat{A} = \widehat{T} = 40^\circ$ (sum of \angle s of Δ) \checkmark A $\therefore \Delta ABC // \Delta TSP$ ($\angle\angle\angle$) \checkmark A	<p>Correct statement with reason: 1 mark</p> <p>Correct statement with reason: 1 mark</p> <p>Correct statement with reason: 1 mark</p> <p>Correct statement with reason: 1 mark</p>	(4)
	8.2.2	$y = AC = 15$ (given) \checkmark A $\frac{PS}{BC} = \frac{TS}{AB} = \frac{PT}{AC}$ (Sides are proportional) \checkmark A $\frac{x}{12} = \frac{5 \times 12}{15}$ $\therefore x = 4$ units \checkmark A	<p>Correct statement with reason: 1 mark</p> <p>Correct statement with reason: 1 mark</p> <p>Answer: 1 mark</p>	(3)
8.3	8.3.1	<i>In ΔABC and ΔDCB</i> 1. $\widehat{A} = \widehat{D}$ (given) \checkmark A 2. $\widehat{ACB} = \widehat{DBC}$ (given) \checkmark A 3. $BC = BC$ (Common) \checkmark A 4. $\Delta ABC \equiv \Delta DCB$ ($\angle\angle S$) \checkmark A	<p>Correct statement with reason: 1 mark</p> <p>Correct statement with reason: 1 mark</p> <p>Correct statement with reason: 1 mark</p> <p>Correct statement with reason: 1 mark</p>	(4)

	8.3.2	$AB = DC$ (From congruency) ✓A $\therefore BC = 4$ units ✓A	Correct statement with reason: 1 mark Answer: 1 mark	(2)
				[23]
QUESTION 9				
	9.1	$P'(-4; -1)$ ✓A $Q'(-1; 3)$ ✓A $R'(4; 1)$ ✓A	Answer: 1 mark Answer: 1 mark Answer: 1 mark	(3)
	9.2	Translation ✓A	Answer: 1 mark	(1)
				[4]
QUESTION 10				
	10.1	$V = \pi r^2 h$ ✓M $= (3,14 \times 7^2) \text{ cm}^2 \times 20) \text{ cm}^1$ ✓M $= 3,14 \times 49 \text{ cm}^2 \times 20 \text{ cm}$ $= 3077,2 \text{ cm}^3$ ✓A	Formula: 1 mark Substitution: 1 mark Answer: 1 mark	(3)
	10.2	In $\triangle DBC$ $DB^2 = 64 + 34 \text{ cm}^2$ (Pythagoras) ✓ M $= 100 \text{ cm}^2$ $= 10 \text{ cm}$ ✓ A In $\triangle ABD$: $AD^2 = (26^2 - 10^2) \text{ cm}^2$ (Pythagoras) ✓ M $= (676 - 100) \text{ cm}^2$ $= 576 \text{ cm}^2$ $\therefore AD = 24 \text{ cm}$ ✓ A	Correct statement with reason: 1 mark 10cm: 1 mark Correct statement with reason: 1 mark Answer: 1 mark	(4)
	10.3	$V = 30 \text{ cm}^3$ (given) Volume when all dimensions are doubled: $V = 10 \text{ cm} \times 6 \text{ cm} \times 4 \text{ cm}$ ✓ M $= \frac{240}{30} \text{ cm}^3$ $= 8$ 8 times ✓ A	Calculation: 1 mark 8 times: 1 mark	(2)
				[9]

QUESTION 11																
11.1	$\text{Tennis} = \frac{12}{48} \times 360^\circ = 90^\circ \quad \checkmark M$ $\text{Rugby} = \frac{18}{48} \times 360^\circ = 135^\circ$ $\text{Cricket} = \frac{6}{48} \times 360^\circ = 45^\circ \quad \checkmark M$ $\text{Swimming} = \frac{12}{48} \times 360^\circ = 90^\circ$ <div style="text-align: center;"> <p>Tennis 90° Swimming 90° Cricket 45° Rugby 135°</p> </div> <p><u>Pie chart showing learners participating in different extra-mural activities</u> $\checkmark A$</p>	<p>Calculation for any two: 1 mark Calculation for any two: 1 mark</p> <p>Pie chart: 1 mark</p> <p>Label: 1 mark</p>	(4)													
11.2	$\text{Range} = 145 - 116$ $= 29 \quad \checkmark A$	Answer: 1 mark	(1)													
11.3	<table border="1" style="margin-left: auto; margin-right: auto;"> <thead> <tr> <th colspan="2" rowspan="2"></th> <th colspan="2">Second toss</th> </tr> <tr> <th>Head</th> <th>Tail</th> </tr> </thead> <tbody> <tr> <th rowspan="2">First toss</th> <th>Head</th> <td>H ; H</td> <td>H ; T</td> </tr> <tr> <th>Tail</th> <td>T ; H</td> <td>T ; T</td> </tr> </tbody> </table> <p style="text-align: center;">$\checkmark \quad \checkmark A$</p>			Second toss		Head	Tail	First toss	Head	H ; H	H ; T	Tail	T ; H	T ; T	<p>Answer: 1 mark</p> <p>Answer: 1 mark</p>	(2)
				Second toss												
		Head	Tail													
First toss	Head	H ; H	H ; T													
	Tail	T ; H	T ; T													
11.3.2	$n(S) = 4 \quad \checkmark A$	Answer: 1 mark	(1)													
11.3.3	$P(\text{at least T}) = \frac{3}{4} \quad \checkmark A$	Answer: 1 mark	(1)													
			[9]													
TOTAL:			100													